# POZNAN UNIVERSITY OF TECHNOLOGY



EUROPEAN CREDIT TRANSFER AND ACCUMULATION SYSTEM (ECTS) pl. M. Skłodowskiej-Curie 5, 60-965 Poznań

# **COURSE DESCRIPTION CARD - SYLLABUS**

Course name		
Number Theory and Cryptography		
Course		
Field of study		Year/Semester
Mathematics in Technology		3/6
Area of study (specialization)		Profile of study
		general academic
Level of study		Course offered in
First-cycle studies		Polish
Form of study		Requirements
full-time		elective
Number of hours		
Lecture	Laboratory classes	Other (e.g. online)
30		
Tutorials	Projects/seminars	
15		
Number of credit points		
4		
Lecturers		
Responsible for the course/lecture	•	Responsible for the course/lecturer:
dr Anna Iwaszkiewicz-Rudoszańska		
email: anna.iwaszkiewicz-		
rudoszanska@put.poznan.pl		
tel. 61 665 2812		
Faculty of Control, Robotics and Ele	ctrical	
Engineering		
Piotrowo 3A, 60-965 Poznań		

#### Prerequisites

Basic knowledge of algebra and discrete mathematics. Basic knowledge of algebra and discrete mathematics. Understanding the necessity of expanding own competences.

#### **Course objective**

The course is intended to present the basic schemes of public key cryptography and results in number theory necessary to understand them.

#### **Course-related learning outcomes**

#### Knowledge

1. Formulates definitions and theorems from number theory used in discussed cryptographic

## POZNAN UNIVERSITY OF TECHNOLOGY



EUROPEAN CREDIT TRANSFER AND ACCUMULATION SYSTEM (ECTS) pl. M. Skłodowskiej-Curie 5, 60-965 Poznań

# algorithms.

2. Explaines basic concepts of public key cryptography and give an account of different cryptosystems.

### Skills

1. Performs calculations necessary for encryption and decryption in discussed cryptographic systems.

2 Uses theorems from number theory and algebra in the analysis of cryptographic systems. Justifies the correctness of selected cryptographic systems.

Social competences

- 1. Knows the limits of her/his own knowledge and understands the need for further education.
- 2. Is aware of the limitations of contemporary cryptography.

### Methods for verifying learning outcomes and assessment criteria

Learning outcomes presented above are verified as follows: Lecture: Written test at the end of semester.

Tutorials: Three short tests during semester.

### Programme content

Lecture: Congruences (Chinese Remainder Theorem, Euler's function, Euler's Theorem). Arithmetic functions. Quadratic residues, Legendre and Jacobi symbols, Gauss' Law of Reciprocity. Primality testing. Discrete logarithm problem. Diffie-Hellman key exchange systems. Public key cryptography. RSA, Rabin's and ElGamal encryption schemes. Signature schemes. Blind signatures. Elliptic Curves. Elliptic curve cryptosystems. Complexity of selected algorithms.

Tutorials: Congruences (Chinese Remainder Theorem. Euler's function, Euler's Theorem). Quadratic residues, Gauss' Law of Reciprocity. Arithmetic in finite fields. RSA, Rabin's and ElGamal encryption schemes. Signature schemes. Elliptic Curves.

### **Teaching methods**

Lectures: lecture with presentation supplemented with proofs and examples on the blackboard, with questions formulating to group; theory presented with connections of current knowledge.

Tutorials: solving on board example tasks, initiating disscussion of solutions.

### Bibliography

Basic

- 1. N. Koblitz, Wykład z teorii liczb i kryptografii, WNT, Warszawa 1995
- 2. W. Marzantowicz, P. Zarzycki, Elementarna teoria liczb, PWN Warszawa 2006
- 3. A.J. Menezes, P.C. van Oorschot, S.A. Vanstone, Kryptografia stosowana, WNT, Warszawa 2005

#### Additional

1. W. Narkiewicz, Teoria liczb, PWN Warszawa 2003

# POZNAN UNIVERSITY OF TECHNOLOGY



EUROPEAN CREDIT TRANSFER AND ACCUMULATION SYSTEM (ECTS) pl. M. Skłodowskiej-Curie 5, 60-965 Poznań

2.W. Sierpiński, Teoria liczb, MM tom 19, IM PAN, Warszawa 1950

3. D.R. Stinson, kryptografia w teorii i w praktyce, WNT, Warszawa 2005

### Breakdown of average student's workload

	Hours	ECTS
Total workload	100	4,0
Classes requiring direct contact with the teacher	45	2,0
Student's own work (literature studies, preparation for tutorials, preparation for tests) <sup>1</sup>	55	2,0

<sup>&</sup>lt;sup>1</sup> delete or add other activities as appropriate